

Oct 19

340 - 120

$$Y(y) = \sum_{n=1}^{\infty} C_n \sin\left(\frac{n\pi}{a}y\right) = V_0$$

$$\int_0^a \sum_{n=1}^{\infty} C_n \sin\left(\frac{n\pi}{a}y\right) \sin\left(\frac{n'\pi}{a}y\right) dy = \int_0^a V_0 \sin\left(\frac{n'\pi}{a}y\right) dy$$

bring  $C_n$  out of integral

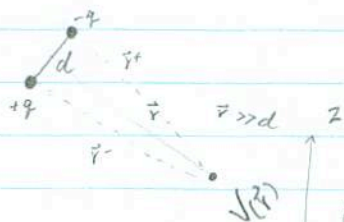
$$\int_0^a \sin\left(\frac{n\pi}{a}y\right) \sin\left(\frac{n'\pi}{a}y\right) dy = \begin{cases} 0 & \text{if } n \neq n' \\ \frac{a}{2} & \text{if } n = n' \end{cases} \rightarrow \frac{a}{2} \delta_{n,n'}$$

$$C_{n'} = \frac{2}{a} \int_0^a V_0 \sin\left(\frac{n'\pi}{a}y\right) dy = \frac{2V_0}{a} \left[ -\cos\left(\frac{n'\pi}{a}y\right) \frac{a}{n'\pi} \right]_0^a$$

$$= \frac{2V_0}{n'\pi} [1 - \cos(n'\pi)] = \frac{4V_0}{n'\pi} \text{ for } n' = 1, 3, 5 \text{ and } 0 \text{ for } n' = 0, 2, 4$$

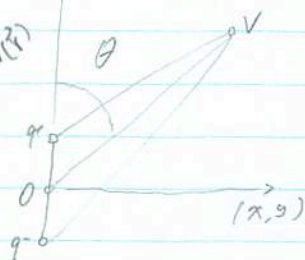
$$V(x, y, z) = \sum_{n=1,3,5}^{\infty} \frac{4V_0}{n\pi} e^{-\frac{n\pi z}{a}} \sin\left(\frac{n\pi y}{a}\right)$$

The Dipole



$$V(r) = \frac{1}{4\pi\epsilon_0} \left( \frac{q}{r^+} + \frac{q}{r^-} \right) = \frac{q}{4\pi\epsilon_0} \left( \frac{1}{r^+} - \frac{1}{r^-} \right)$$

must define a coordinate



$$\text{then we have } V(r) = \frac{q}{4\pi\epsilon_0} \frac{d}{r^2} \cos\theta$$

a dipole has a direction  $|\vec{P}| = qd$ 

so

$$V(r) = \frac{1}{4\pi\epsilon_0} \frac{\vec{P} \cdot \hat{r}}{r^2}$$

$$\vec{E}(r) = -\vec{\nabla} V(r) = -\left[ \frac{\partial}{\partial r} \hat{r} + \frac{1}{r} \frac{\partial}{\partial \theta} \hat{\theta} + \frac{1}{r \sin\theta} \frac{\partial}{\partial \phi} \hat{\phi} \right] \frac{1}{4\pi\epsilon_0} \frac{P \cos\theta}{r^2}$$

$$= \frac{P}{4\pi\epsilon_0 r^3} (2 \cos\theta \hat{r} + \sin\theta \hat{\theta})$$

Hilroy